



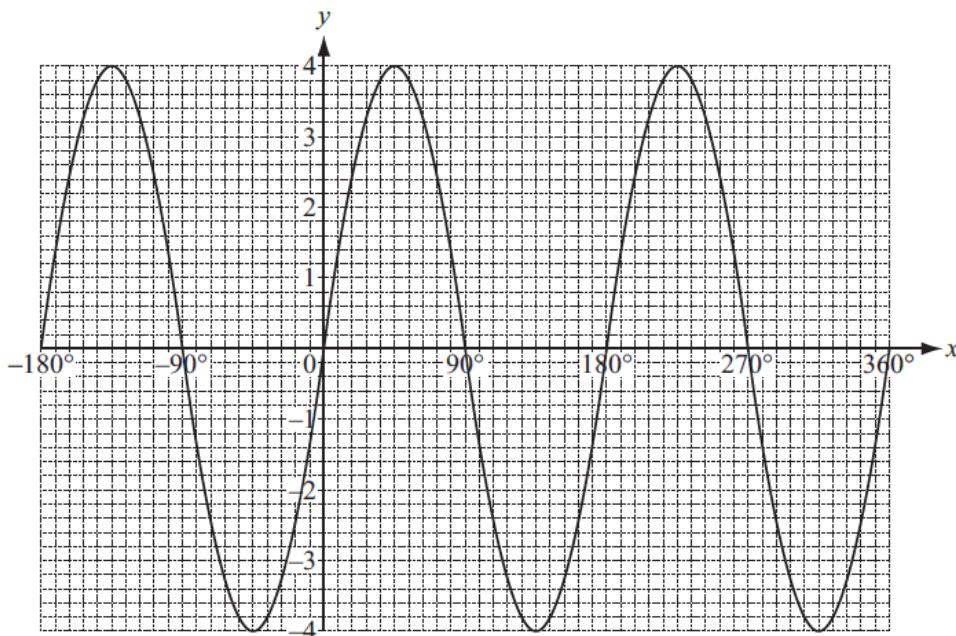
8.8 – Graphs of Trigonometric functions

Student name: _____ **Answers** _____ Score: _____

1. For the function $f(x) = 2\sin 3x$ write down

- (a) The amplitude **2** [1]
(b) The period **120** [1]

2.



The diagram shows the graph of $y = f(x)$, where $f(x) = a\sin(bx)$.

Find the values of a and b .

$$a = \dots \textcolor{red}{4} \dots \quad [1]$$
$$b = \dots \textcolor{red}{2} \dots \quad [1]$$

3. For $0^\circ < x < 360^\circ$ find the values of x that satisfy the equation $\cos x = -\frac{1}{2}$.

$$x = \dots \textcolor{red}{120} \dots \text{ and } x = \dots \textcolor{red}{240} \dots \quad [2]$$

4. Describe fully the **single** transformation that maps the graph of $y = \cos x$ onto the graph of $y = 3\cos x$.

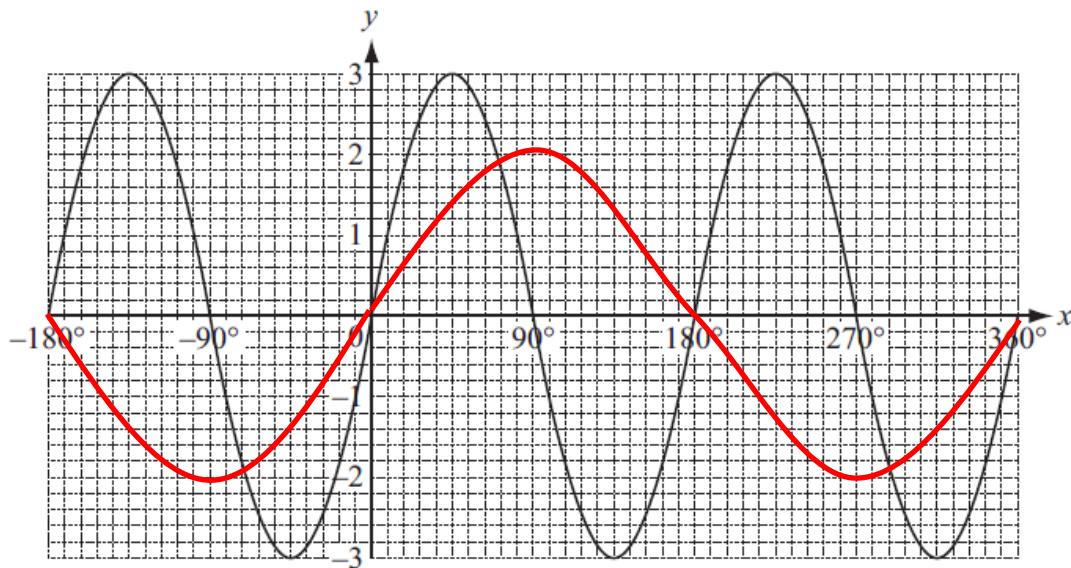
..... **Stretch, x -axis invariant line, stretch factor 3**

5. $f(x) = 6\cos(6x)$

Find the amplitude and the period of $f(x)$.

$$\text{amplitude} = \dots \textcolor{red}{6} \dots$$
$$\text{period} = \dots \textcolor{red}{60} \dots \quad [2]$$

6.



- (a) Write down the equation of the graph.

$$y = 3 \sin 2x \dots [2]$$

- (b) On the same axes above sketch the graph of $y = 2 \sin x$ for $-180^\circ \leq x \leq 360^\circ$.

[2]

7. (a) For the function $y = 3\sin 2x$ write down

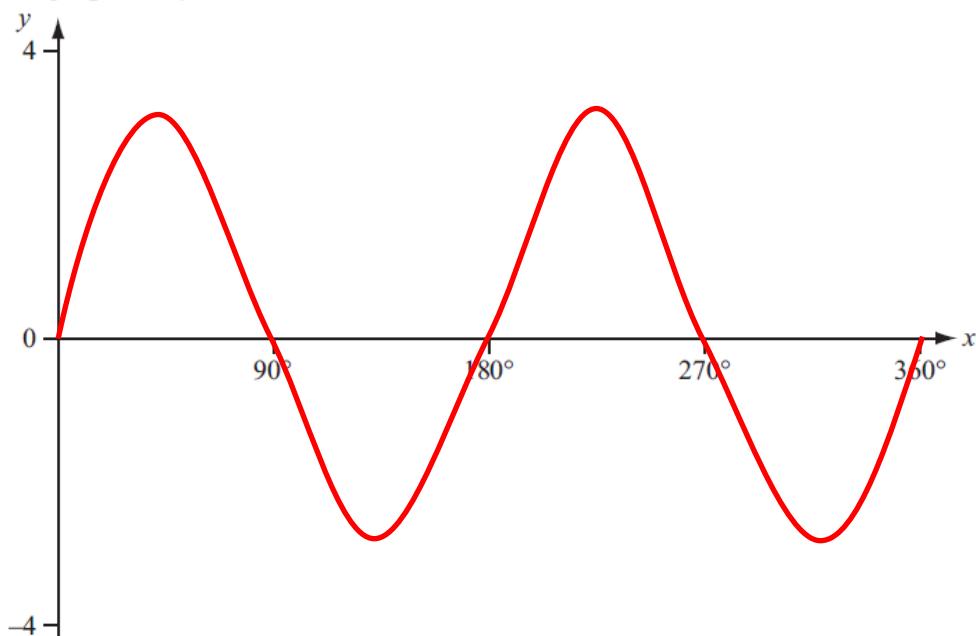
- (i) the amplitude,

$$\dots \text{3} \dots [1]$$

- (ii) the period.

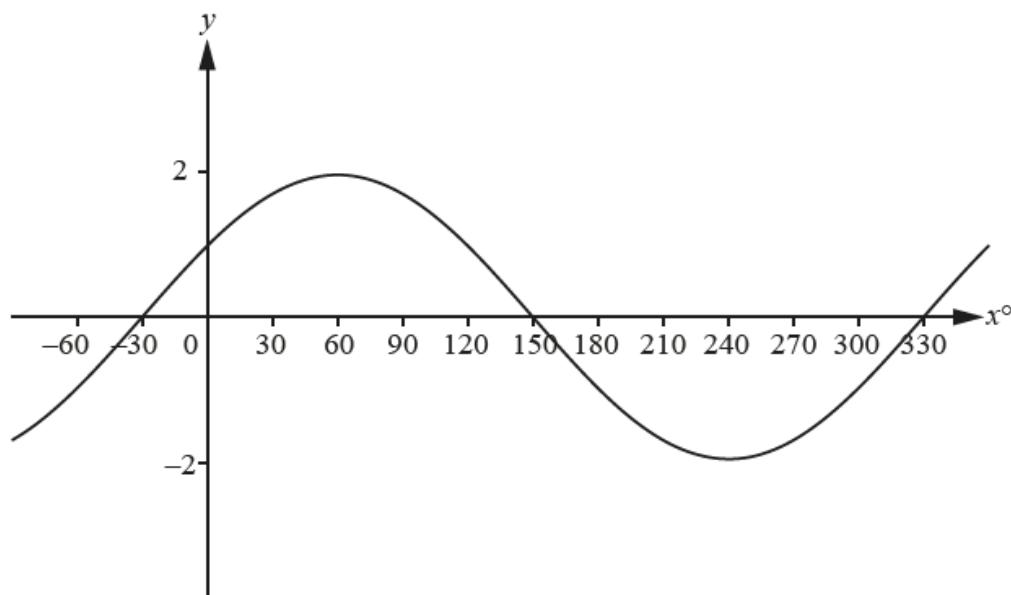
$$\dots \text{180 or } \pi \dots [1]$$

- (b) Sketch the graph of $y = 3\sin 2x$ on the axes below for $0^\circ \leq x \leq 360^\circ$.



[2]

8.



The graph of $y = a \sin(x + b)^\circ$ is shown in the diagram.
Find the value of a and the value of b .

$$a = \dots \textcolor{red}{2} \dots \dots \dots$$

$$b = \dots \textcolor{red}{30} \dots \dots \dots [1]$$

9. (a) Find the amplitude and period of the function $f(x) = 4 \cos(4x)$.

$$\text{amplitude} = \dots \textcolor{red}{4} \dots \dots \dots$$

$$\text{period} = \dots \textcolor{red}{90} \dots \dots \dots [2]$$

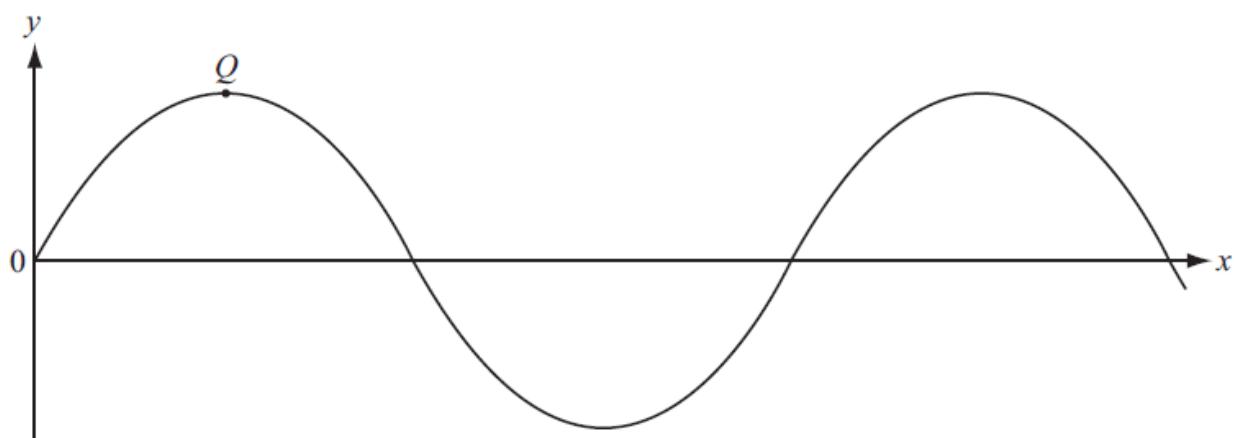
(b) $g(x) = 4 \cos(4x) - 4$

Describe fully the single transformation that maps the graph of $y = f(x)$ onto the graph of $y = g(x)$.

$\text{Translation } \begin{pmatrix} 0 \\ -4 \end{pmatrix}$

..... [2]

10.



The diagram shows the graph of $y = 3 \sin 2x$.
 Q is a local maximum point.

Find the co-ordinates of Q .

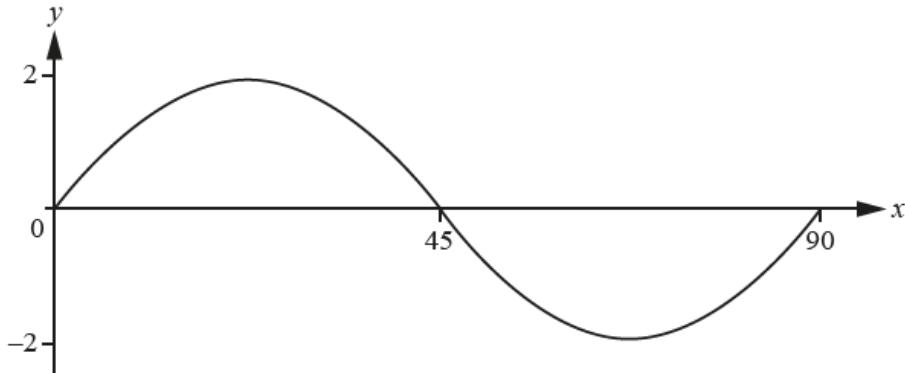
$$(\dots \textcolor{red}{45} \dots \dots \dots, \dots \textcolor{red}{3} \dots \dots \dots) [2]$$

- 11.** The graph of $y = a \cos(bx)^\circ$ has a maximum point at $(360, 3)$ and a minimum point at $(450, -3)$.

Find the value of a and the value of b .

- (a) 3
(b) 2 [2]

12.



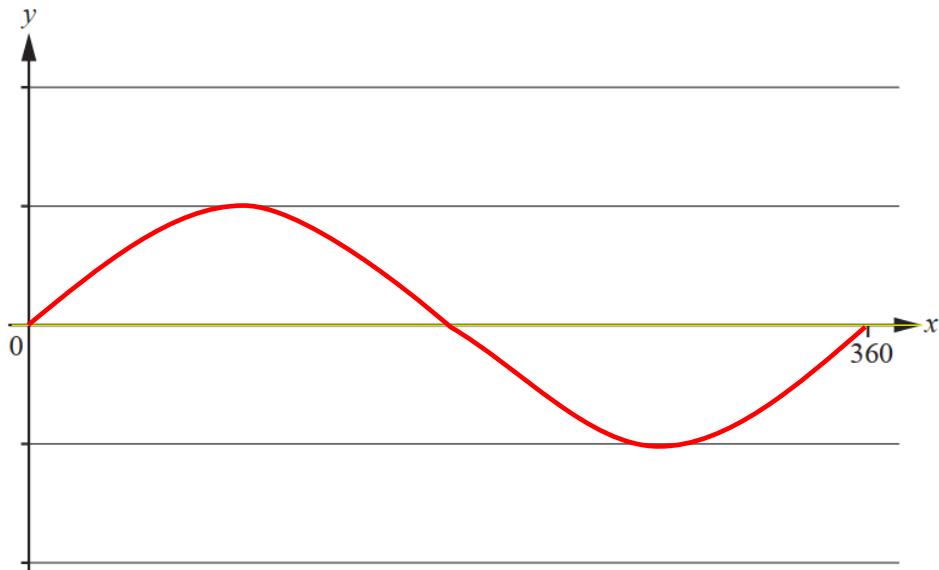
The diagram shows the graph of $y = a \sin(bx)^\circ$, for $0 \leq x \leq 90$.

Find the value of a and the value of b .

$$q \equiv \dots^{\color{red}2}$$

$b = \dots$

13. (a) On the grid, sketch the graph of $y = \sin x^\circ$ for $0 \leq x \leq 360$.



[2]

- (b) The point $(a, 0.5)$ is on the graph of $y = \sin x^\circ$.

Find the two possible values of a .

$$a = \dots 30 \dots \text{ or } a = \dots 150 \dots [2]$$



14. $f(x) = 3 \sin 2x^\circ$

- (a) Write down the amplitude of the graph of $f(x)$.

..... **3** [1]

- (b) The graph of $y = f(x)$ goes through the points $(75, 1.5)$ and $(a, 1.5)$.

Find a possible value of a , greater than 75.

195 or 255 or 375 or 435, etc [1]