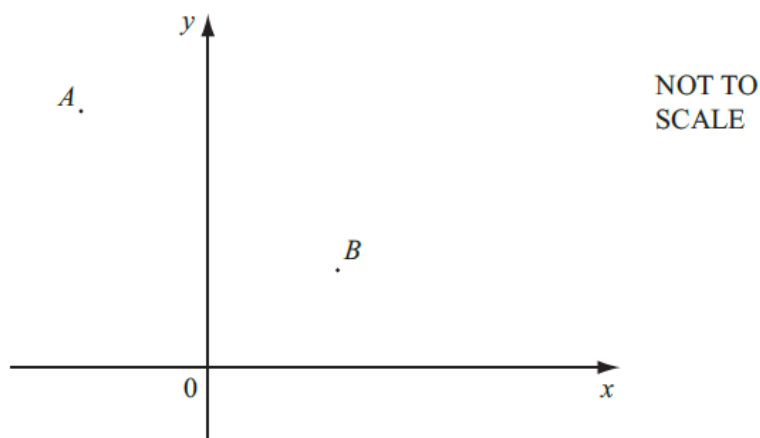




6 – Vectors

Student name: _____ Score: _____

1. The points $A(-3, 5)$ and $B(3, 2)$ are shown on the diagram below.



- (a) (i) Write down the vector $\vec{AB}$ in component form.

$\left(\quad \right)$ [2]

- (ii) Find $|\vec{AB}|$ leaving your answer in surd form.

..... [2]

- (b) Calculate the gradient of the line AB .

..... [2]

- (c) Calculate the co-ordinates of the midpoint of the line AB .

(.....,) [1]

- (d) Find the equation of the perpendicular bisector of the line AB .

..... [2]

2. $\mathbf{p} = \begin{pmatrix} 5 \\ 1 \end{pmatrix}$ and $\mathbf{q} = \begin{pmatrix} -4 \\ 2 \end{pmatrix}$

- (a) Write $2\mathbf{p} - \frac{1}{2}\mathbf{q}$ as a column vector.

$\left(\quad \right)$ [2]

- (b) Find $|\mathbf{q}|$ leaving your answer in surd form.

..... [2]

3. $\mathbf{p} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$ $\mathbf{q} = \begin{pmatrix} -4 \\ 3 \end{pmatrix}$

- (a) Find $2\mathbf{p} - 3\mathbf{q}$.

$\left(\quad \right)$ [2]

- (b) Calculate $|\mathbf{q}|$.

..... [2]

4. $\mathbf{p} = \begin{pmatrix} -2 \\ 3 \end{pmatrix}$ $\mathbf{q} = \begin{pmatrix} 5 \\ -7 \end{pmatrix}$

(a) Find $\mathbf{p} + \mathbf{q}$.

$$\begin{pmatrix} \\ \end{pmatrix}$$

[2]

(b) Work out $|\mathbf{p} + \mathbf{q}|$.

..... [2]

5. $\mathbf{p} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$ $\mathbf{q} = \begin{pmatrix} -3 \\ 5 \end{pmatrix}$

Find

(a) $2\mathbf{p} - 3\mathbf{q}$,

$$\begin{pmatrix} \\ \end{pmatrix}$$

[2]

(b) $|\mathbf{p}|$.

..... [2]

6. Find the magnitude of $\begin{pmatrix} -6 \\ 4 \end{pmatrix}$.

Write your answer in surd form as simply as possible.

..... [3]

7. $\mathbf{a} = \begin{pmatrix} 3 \\ -2 \end{pmatrix}$ $\mathbf{b} = \begin{pmatrix} -2 \\ 5 \end{pmatrix}$

When $2\mathbf{a} + k\mathbf{b} = \begin{pmatrix} -2 \\ 16 \end{pmatrix}$ find the value of k .

..... [3]

8. The line $2x + 3y = 36$ intersects the x -axis at P and the y -axis at Q .
 M is the midpoint of PQ .

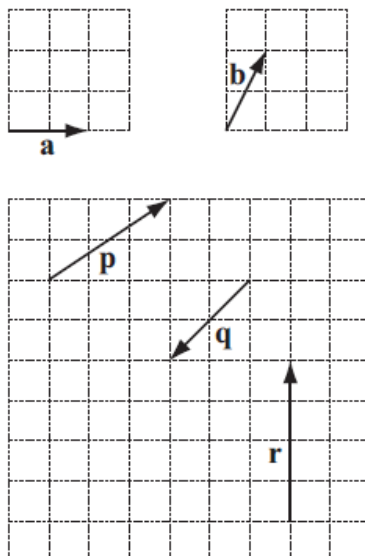
Find the column vector $\overrightarrow{OM}$ where O is the origin.

$$\begin{pmatrix} \\ \end{pmatrix}$$

[4]



9.



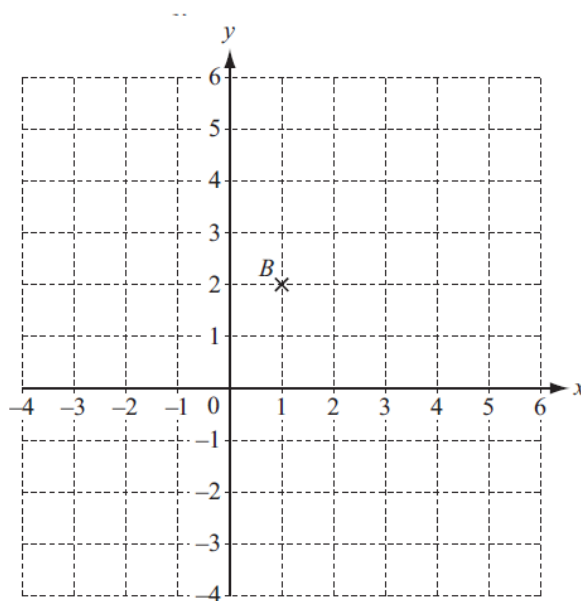
Write the vectors p , q and r in terms of a and b .

$p = \dots\dots\dots$

$q = \dots\dots\dots$

$r = \dots\dots\dots$ [3]

10. (a)



B is the point $(1, 2)$ and $\vec{BC} = \begin{pmatrix} 4 \\ -3 \end{pmatrix}$.

Plot the point C on the grid.

[1]

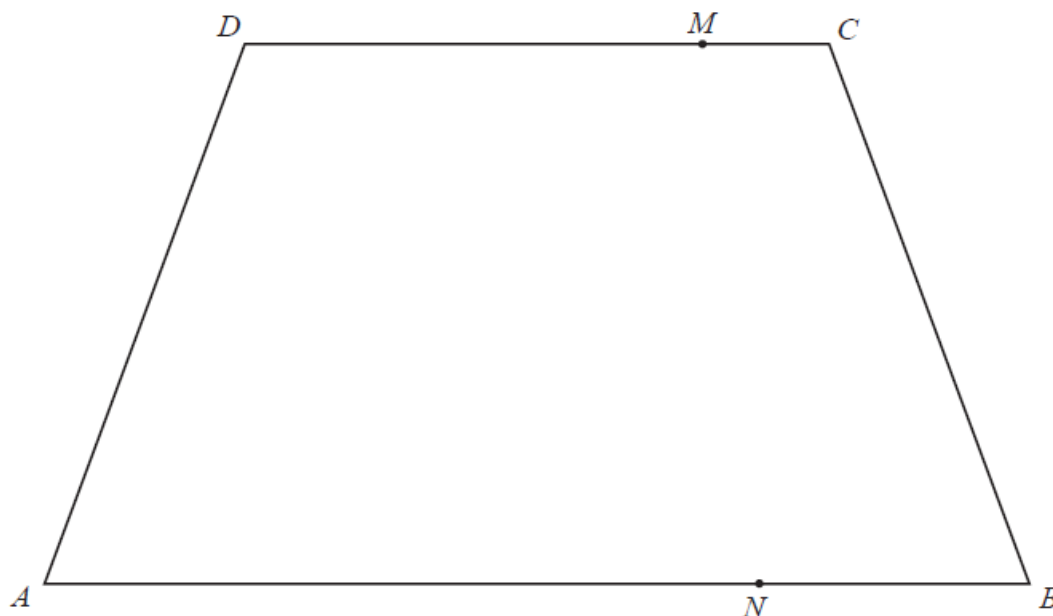
(b) $p = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$ $q = \begin{pmatrix} 4 \\ -1 \end{pmatrix}$.

Write $2p - q$ as a column vector.

$\begin{pmatrix} \\ \end{pmatrix}$

[2]

11.



NOT TO
SCALE

$ABCD$ is a trapezium.

$AB = 2DC$, $DM = 2MC$ and $AN = 3NB$.

$\vec{AB} = \mathbf{p}$ and $\vec{AD} = \mathbf{q}$.

(a) Write $\vec{MC}$ in terms of $\mathbf{p}$.

..... [2]

(b) Find $\vec{MN}$ in terms of $\mathbf{p}$ and $\mathbf{q}$.

..... [2]

12.

$$\mathbf{a} = \begin{pmatrix} 5 \\ -12 \end{pmatrix} \quad \mathbf{b} = \begin{pmatrix} 2 \\ -3 \end{pmatrix}$$

(a) Find $\mathbf{a} - 3\mathbf{b}$.

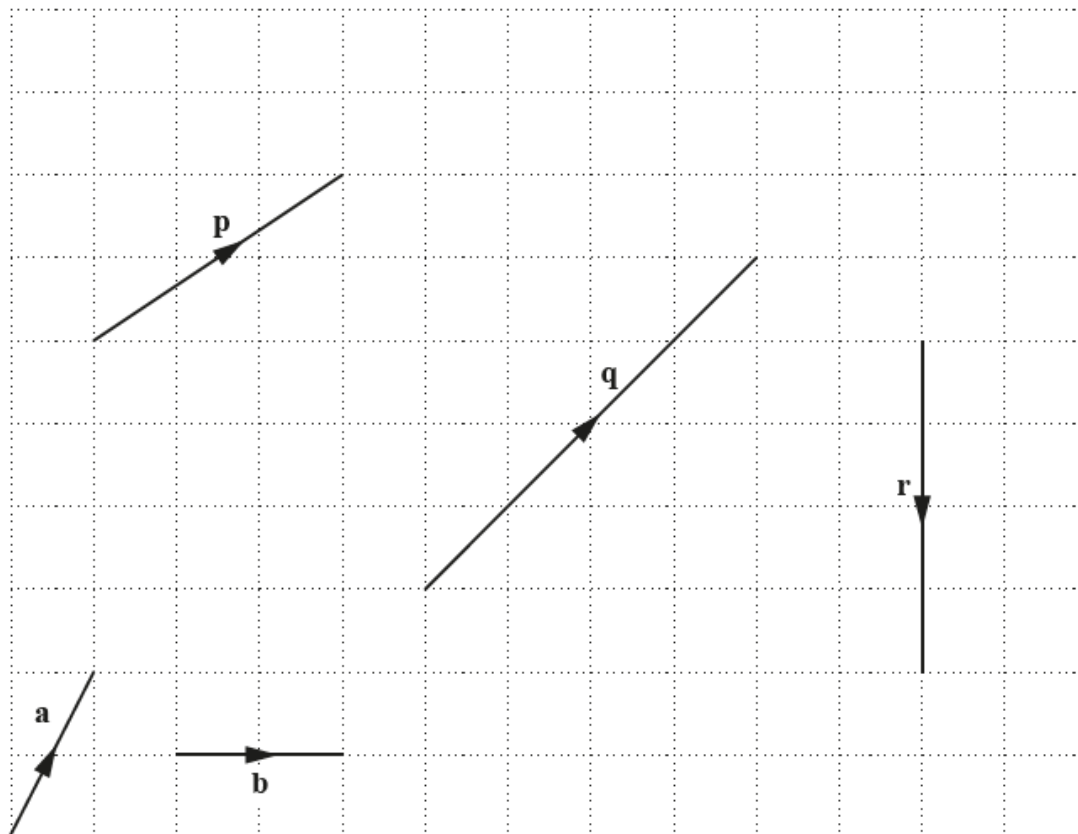
$\begin{pmatrix} \\ \end{pmatrix}$

[2]

(b) Work out $|\mathbf{a}|$.

$|\mathbf{a}| = \dots\dots\dots$ [2]

13.



Write the vectors **p**, **q** and **r** in terms of **a** and **b**.

$p = \dots\dots\dots$
 $q = \dots\dots\dots$
 $r = \dots\dots\dots$ [3]

14. $\mathbf{i} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$ $\mathbf{j} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$ $\mathbf{a} = \begin{pmatrix} 4 \\ -6 \end{pmatrix}$

(a) $\mathbf{a} = p\mathbf{i} + q\mathbf{j}$

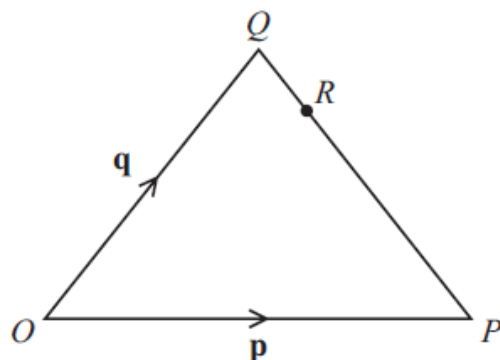
Find the values of p and q .

$p = \dots\dots\dots$
 $q = \dots\dots\dots$ [2]

(b) Calculate $|\mathbf{a}|$, giving your answer in the form $m\sqrt{n}$ where m and n are prime numbers.

$|\mathbf{a}| = \dots\dots\dots$ [3]

15.



NOT TO
SCALE

The diagram shows the vectors $\vec{OP} = \mathbf{p}$ and $\vec{OQ} = \mathbf{q}$.

R is on QP such that $QR = \frac{1}{4} QP$.

Find the following vectors in terms of $\mathbf{p}$ and $\mathbf{q}$.

Give each answer in its simplest form.

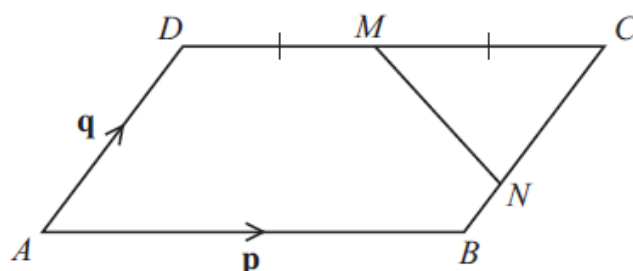
(a) $\vec{PQ}$

$\vec{PQ} = \dots\dots\dots [1]$

(b) $\vec{OR}$

$\vec{OR} = \dots\dots\dots [2]$

16.



NOT TO
SCALE

$ABCD$ is a parallelogram.

$DM = MC$ and $CN = 2NB$.

$\vec{AB} = \mathbf{p}$ and $\vec{AD} = \mathbf{q}$.

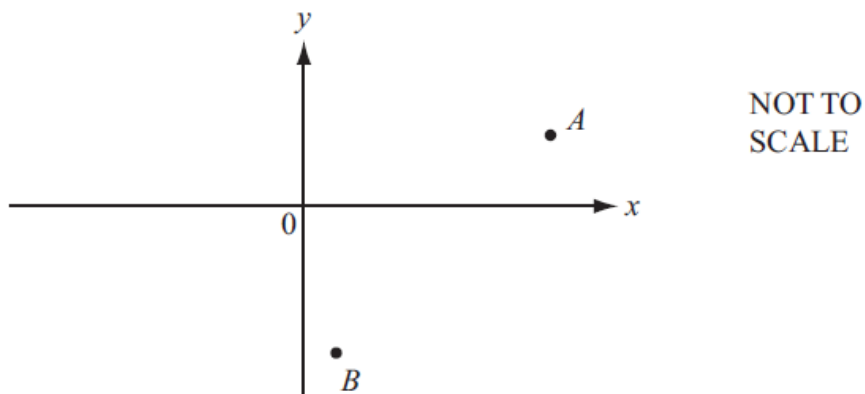
(a) Write down $\vec{CN}$ in terms of $\mathbf{q}$.

$\vec{CN} = \dots\dots\dots [1]$

(b) Find $\vec{MN}$ in terms of $\mathbf{p}$ and $\mathbf{q}$.

$\vec{MN} = \dots\dots\dots [1]$

17. (a)



A is the point $(4, 2)$ and B is the point $(1, -3)$.

(i) Write down the vector $\vec{BA}$ in component form.

$$\vec{BA} = \begin{pmatrix} \\ \end{pmatrix}$$

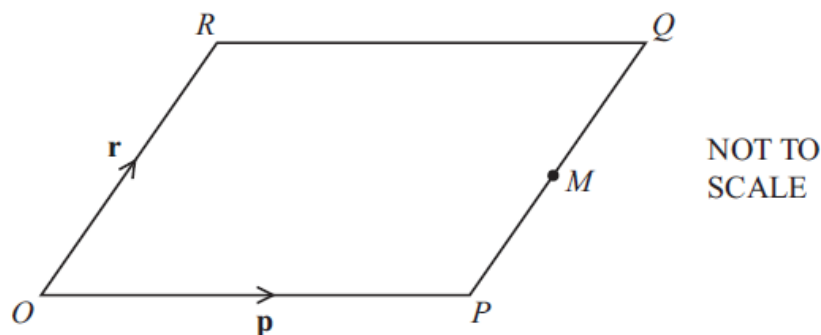
[1]

(ii) $\vec{BC} = \begin{pmatrix} -3 \\ 4 \end{pmatrix}$

Write down the co-ordinates of C .

(.....,) [1]

(b)



$OPQR$ is a parallelogram and M is the midpoint of PQ .

$\vec{OP} = \mathbf{p}$ and $\vec{OR} = \mathbf{r}$.

Find $\vec{OM}$ in terms of $\mathbf{p}$ and $\mathbf{r}$.

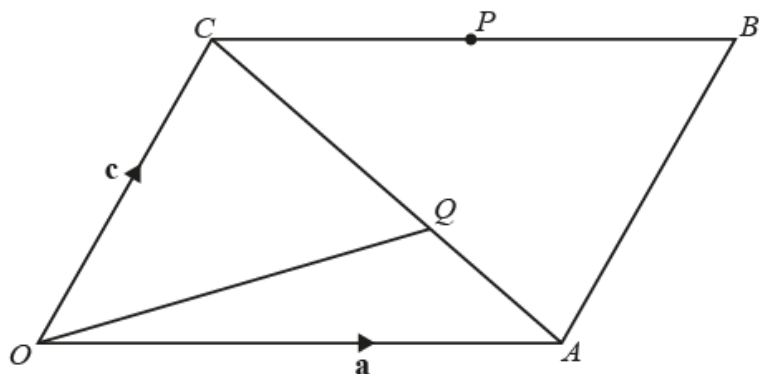
$$\vec{OM} = \dots\dots\dots [2]$$

18. $\mathbf{p} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$ $\mathbf{q} = \begin{pmatrix} 1 \\ 6 \end{pmatrix}$

Find $2\mathbf{p} - 3\mathbf{q}$.

..... [2]

19.



NOT TO
SCALE

$OABC$ is a parallelogram.
 P is the midpoint of CB .
 $CQ : QA = 5 : 3$.

$\overrightarrow{OA} = \mathbf{a}$ and $\overrightarrow{OC} = \mathbf{c}$.

Find these vectors in terms of $\mathbf{a}$ and/or $\mathbf{c}$, giving your answers in their simplest form.

(a) $\overrightarrow{CP}$

$\overrightarrow{CP} = \dots\dots\dots$ [1]

(b) $\overrightarrow{OQ}$

$\overrightarrow{OQ} = \dots\dots\dots$ [3]

20.

$$p = \begin{pmatrix} 6 \\ 3 \end{pmatrix}$$

Find $|p|$, giving your answer in the form $3\sqrt{a}$.

$|p| = \dots\dots\dots$ [2]

21. Q is the point $(3, 7)$ and $\overrightarrow{PQ} = \begin{pmatrix} -6 \\ 3 \end{pmatrix}$.

(a) Find the co-ordinates of P .

$(\dots\dots\dots, \dots\dots\dots)$ [2]

(b) Find $|\overrightarrow{PQ}|$.
 Give your answer in its simplest surd form.

$\dots\dots\dots$ [3]

22. A is the point $(1, 5)$ and B is the point $(6, 2)$.

Find the column vector $\overrightarrow{AB}$.

$$\begin{pmatrix} \\ \end{pmatrix}$$

[2]



23. $\mathbf{a} = \begin{pmatrix} 6 \\ 8 \end{pmatrix}$ $\mathbf{b} = \begin{pmatrix} 2 \\ -8 \end{pmatrix}$

(a) Find $\mathbf{a} - 3\mathbf{b}$.

$\left(\quad \right)$

[2]

(b) Work out $|\mathbf{a}|$.

..... [2]

24. $\mathbf{p} = \begin{pmatrix} 3 \\ -1 \end{pmatrix}$ $\mathbf{q} = \begin{pmatrix} 1 \\ -2 \end{pmatrix}$

(a) Find $\mathbf{p} + \mathbf{q}$.

$\left(\quad \right)$

[1]

(b) A is the point $(2, 7)$.

The point A is translated to the point B by the vector $\mathbf{p} + \mathbf{q}$.

Find the coordinates of B .

(.....,) [2]

25.(a) Work out $\begin{pmatrix} 12 \\ -5 \end{pmatrix} - 5\begin{pmatrix} 4 \\ -1 \end{pmatrix}$.

$\left(\quad \right)$

[2]

(b) Work out the magnitude of $\begin{pmatrix} 3 \\ -4 \end{pmatrix}$.

..... [2]

26. Work out $4 \times \begin{pmatrix} 6 \\ -2 \end{pmatrix}$.

$\left(\quad \right)$

[1]

27. Find the magnitude of the vector $\begin{pmatrix} 2 \\ 6 \end{pmatrix}$.

Give your answer in simplest surd form.

..... [2]

28. $\mathbf{a} = \begin{pmatrix} 4 \\ -10 \end{pmatrix}$ $\mathbf{b} = \begin{pmatrix} -4 \\ 2 \end{pmatrix}$

Find the magnitude of the vector $\mathbf{a} - \mathbf{b}$.

Give your answer in its simplest surd form.

..... [4]

29. A is the point $(1, 3)$ and B is the point $(4, 9)$.

Find $\overrightarrow{AB}$.

$$\overrightarrow{AB} = \begin{pmatrix} \\ \end{pmatrix}$$

[2]

30. $\mathbf{p} = \begin{pmatrix} -3 \\ 5 \end{pmatrix}$

(a) Find the column vector $3\mathbf{p}$.

$$\begin{pmatrix} \\ \end{pmatrix}$$

[1]

(b) Find $|\mathbf{p}|$, giving your answer in surd form.

..... [2]

31. $\mathbf{p} = \begin{pmatrix} 12 \\ -5 \end{pmatrix}$

Find

(a) $2\mathbf{p}$,

$$\begin{pmatrix} \\ \end{pmatrix}$$

[1]

(b) $|\mathbf{p}|$.

..... [2]

32. $\mathbf{a} = \begin{pmatrix} -4 \\ -3 \end{pmatrix}$ $\mathbf{b} = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$

(a) Find $\mathbf{a} - 3\mathbf{b}$.

$$\begin{pmatrix} \\ \end{pmatrix}$$

[2]

(b) Find the magnitude of $\begin{pmatrix} -4 \\ -3 \end{pmatrix}$.

..... [2]

