

Annual depreciation and inflation

Student name: ______ Score: _____

1. Gabriella purchases a new car.

The car's value in dollars, V, is modelled by the function

$$V(t) = 12870 - k(1.1)^t, t \ge 0$$

where t is the number of years since the car was purchased and k is a constant.

(a) Write down, and simplify, an expression for the car's value when Gabriella purchased it.

[2]

After two years, the car's value is \$9143.20.

(b) Find the value of k.

[2]

This model is defined for $0 \le t \le n$. At n years the car's value will be zero dollars.

(c) Find the value of n.

[2]

- 2. In 2000 Herman joined a tennis club. The fees were £ 1200 a year. Each year the fees increase by 3 %.
 - (a) Calculate, to the nearest £ 1, the fees in 2002.
 - (b) Calculate the total fees for Herman who joined the tennis club in 2000 and remained a member for five years.
- 3. The value of a car decreases each year. This value can be calculated using the function

$$v = 32\ 000\ r^t$$
, $t \ge 0$, $0 < r < 1$,

where v is the value of the car in USD, t is the number of years after it was first bought and r is a constant.

- (a) (i) Write down the value of the car when it was first bought.
 - (ii) One year later the value of the car was 27200 USD. Find the value of r.
- (b) Find how many years it will take for the value of the car to be less than 8000 USD.
- **4.** Kylie bought a car for 1200 AUD which depreciated at a rate of r % per year. The value of the car after 7 years is 669 AUD.

Find the rate of depreciation.

[3]

- 5. The rate of inflation from the beginning of 1995 has been 4.5% per year.
 - (a) A loaf of bread cost \$1.70 on January 1, 1996. What did it cost on January 1, 1999?
 - (b) A car cost \$40 000 on January 1, 1999. What did it cost on January 1, 1997? (Give your answer to the nearest thousand dollars.)
- 6. Mario has spent \$40000 to buy some land. The land increases in value by 5% each year.
 - (i) What is the value of the land after the end of five years?

At the end of five years, Mario sells the land. He pays 1% tax on the sale and spends the rest of the money on a car. The car loses value at a rate of \$2500 every year.

- (ii) How much tax does Mario pay?
- (iii) How much is the car worth five years after Mario buys it?





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Student name: _____ Score: ____

1. Gabriella purchases a new car.

The car's value in dollars, V, is modelled by the function

$$V(t) = 12870 - k(1.1)^t, t \ge 0$$

where t is the number of years since the car was purchased and k is a constant.

(a) Write down, and simplify, an expression for the car's value when Gabriella purchased it. 12.870 - k

[2]

After two years, the car's value is \$9143.20.

(b) Find the value of k.

3080

[2]

This model is defined for $0 \le t \le n$. At n years the car's value will be zero dollars.

(c) Find the value of n.

15

[2]

- 2. In 2000 Herman joined a tennis club. The fees were £ 1200 a year. Each year the fees increase by 3 %.
 - (a) Calculate, to the nearest £ 1, the fees in 2002. 1273
 - (b) Calculate the total fees for Herman who joined the tennis club in 2000 and remained a member for five years. 6370.96
- 3. The value of a car decreases each year. This value can be calculated using the function

$$v = 32\ 000\ r^t$$
, $t \ge 0$, $0 < r < 1$,

where v is the value of the car in USD, t is the number of years after it was first bought and r is a constant.

- (a) (i) Write down the value of the car when it was first bought. 32 000
 - (ii) One year later the value of the car was 27200 USD. Find the value of r. 0.85
- (b) Find how many years it will take for the value of the car to be less than 8000 USD.8.53 (9)
- **4.** Kylie bought a car for 1200 AUD which depreciated at a rate of r % per year. The value of the car after 7 years is 669 AUD.

Find the rate of depreciation.

8.01%

[3]



- 5. The rate of inflation from the beginning of 1995 has been 4.5% per year.
 - (a) A loaf of bread cost \$1.70 on January 1, 1996. What did it cost on January 1, 1999? \$1.94
 - (b) A car cost \$40 000 on January 1, 1999. What did it cost on January 1, 1997? (Give your answer to the nearest thousand dollars.) 37 000
- 6. Mario has spent \$40000 to buy some land. The land increases in value by 5% each year.
 - (i) What is the value of the land after the end of five years? 51 051.26

At the end of five years, Mario sells the land. He pays 1% tax on the sale and spends the rest of the money on a car. The car loses value at a rate of \$2500 every year.

- (ii) How much tax does Mario pay? 510.51
- (iii) How much is the car worth five years after Mario buys it? 38 040.75

